



Superfluid ^3He in Motion: from Vortices to Time Crystals



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EPSRC

Engineering and Physical Sciences
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Aalto University
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Technology
Facilities Council

EMP European Microkelvin Platform





Superfluid ^3He in Motion: from Vortices to Time Crystals

Aalto: P.J. Heikkinen, J. Hosio, T. Kamppinen, J.T. Mäkinen, J. Nissinen, V.V. Zavjalov, G.E. Volovik, V.B. Eltsov, M. Krusius

Moscow: A.A. Soldatov, A.N. Yudin, V.V. Dmitriev

Please find our papers on [arXiv](#)



Superfluid ^3He in Motion: from Vortices to Time Crystals

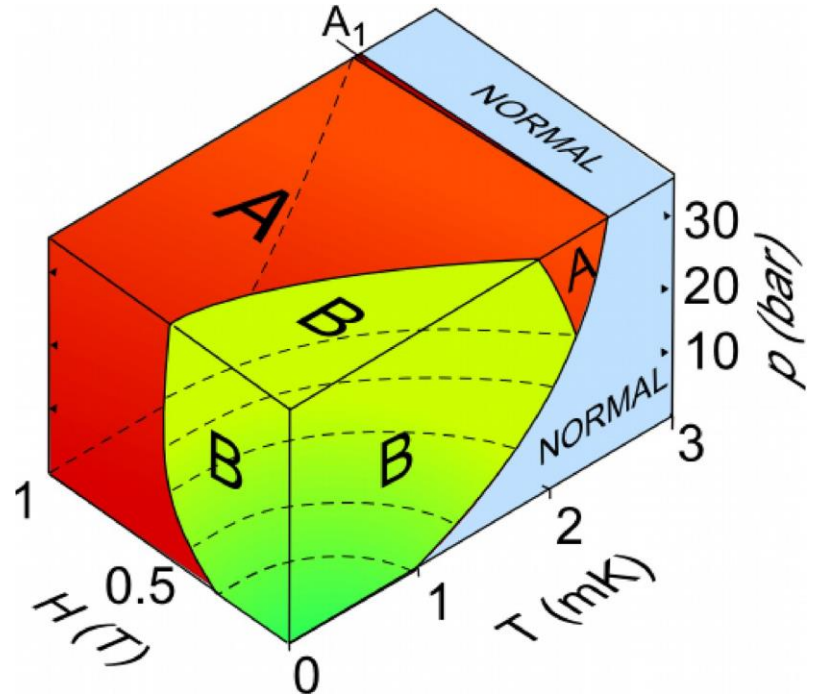
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Superfluid ^3He ?

1. Fermions, so no BEC
--> Cooper pairs as in superconductors?
2. Hard core repulsion
3. P-wave pairing, $S=1$ and $L=1$
4. Order parameter describing S, L, Δ, ϕ



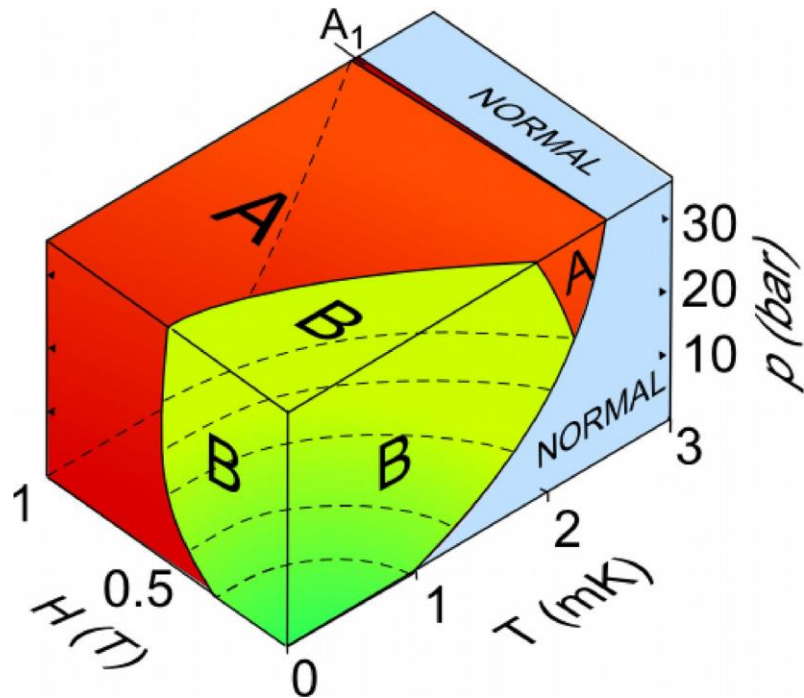
Outline

1. Fermions, so no BEC
--> Cooper pairs as in superconductors?
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3. P-wave pairing, $S=1$ and $L=1$
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Vortices in the polar phase

Kibble-Zurek mechanism with drive and bias

From HPD to interacting time crystals



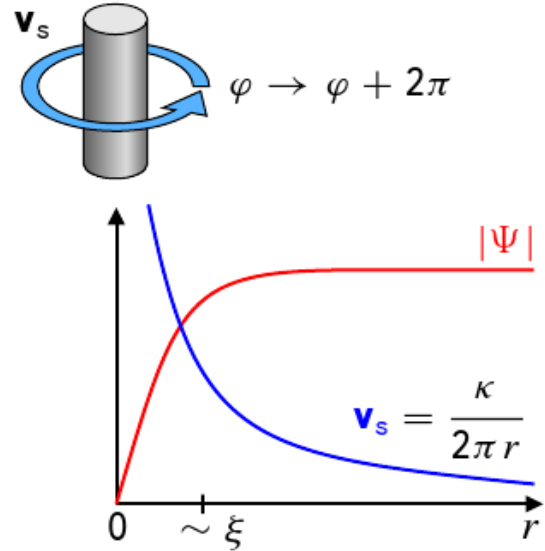
Quantised Vortex?

Order parameter $\psi = |\Psi|e^{i\phi}$, superfluid velocity $v_s = \frac{\hbar}{M} \nabla\phi$
No rotation: $|\Psi| > 0 \Rightarrow \nabla \times v_s \equiv 0$, however,
circulation is allowed via vortices.

Circulation is quantised $\int v_s \cdot dr = \kappa = \frac{2\pi\hbar}{M}$

Core size \sim coherence length ξ

Volovik in 1976: **half-quantum vortices** exist!
- but attempts to resolve in the A phase failed

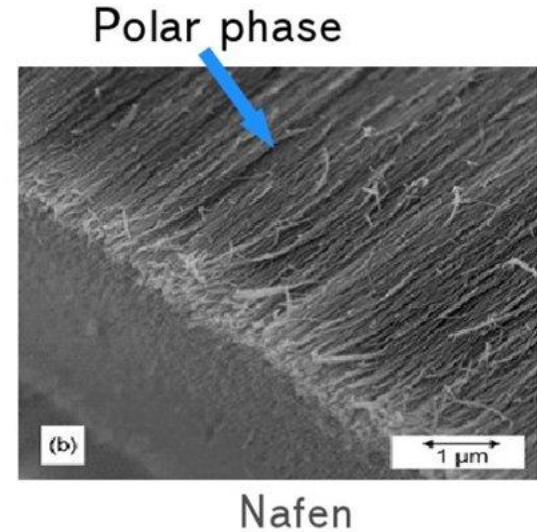


$|\Psi| \rightarrow 0$: **singular** vortex

Polar phase

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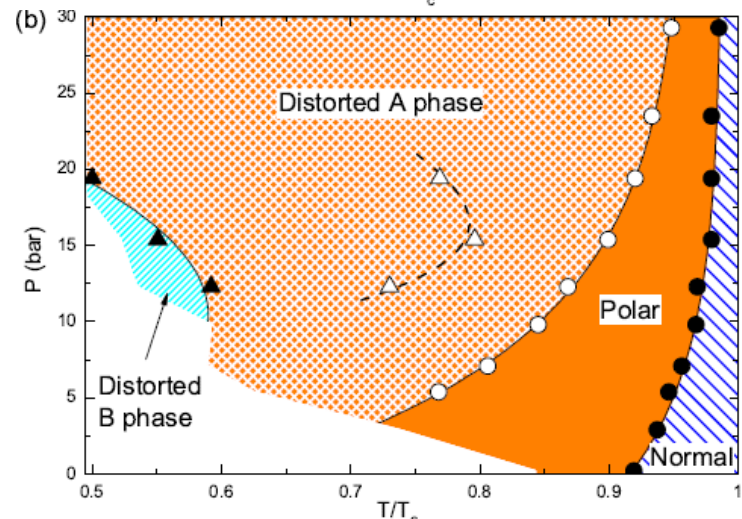
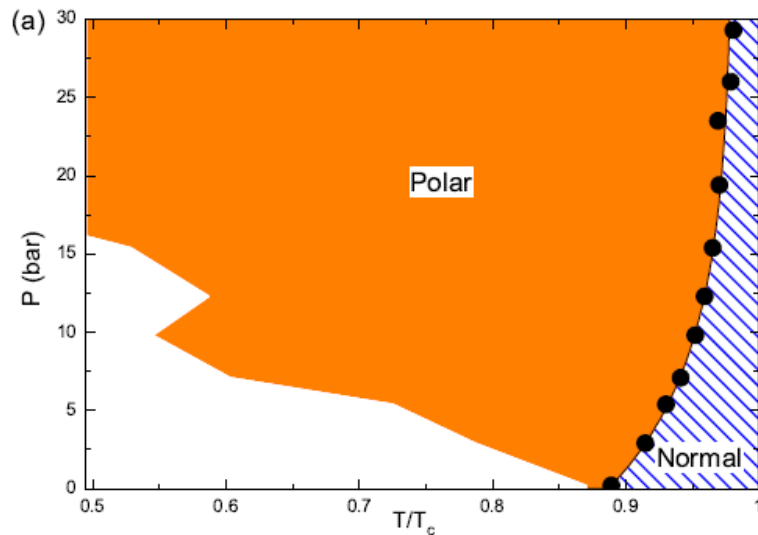
Additional phases in restricted geometries
--> polar phase in 2015



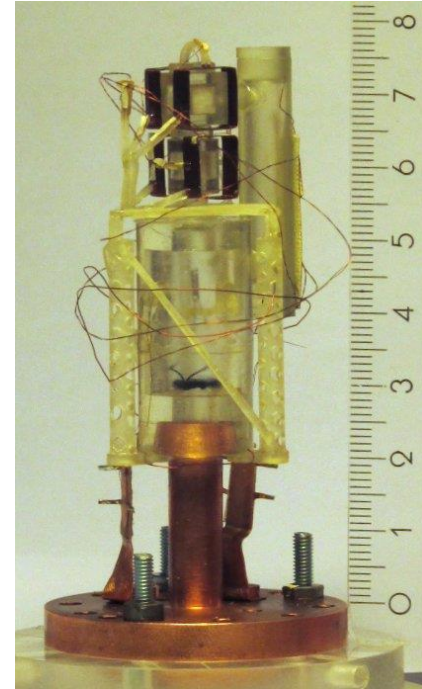
Polar phase

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Additional phases in restricted geometries
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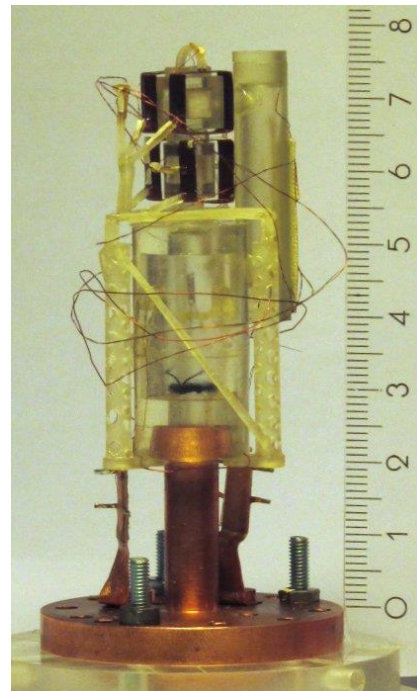
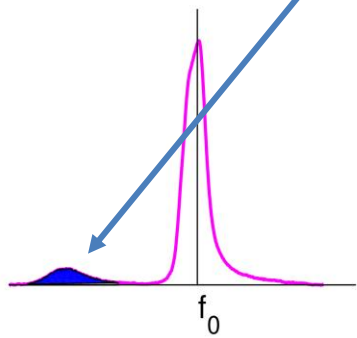
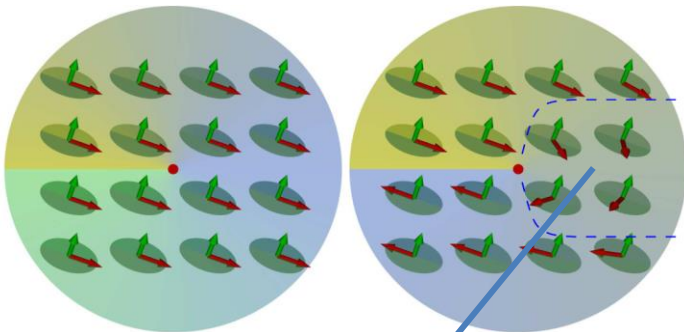
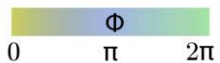
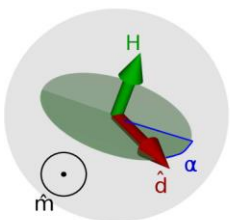


Half-quantum vortex

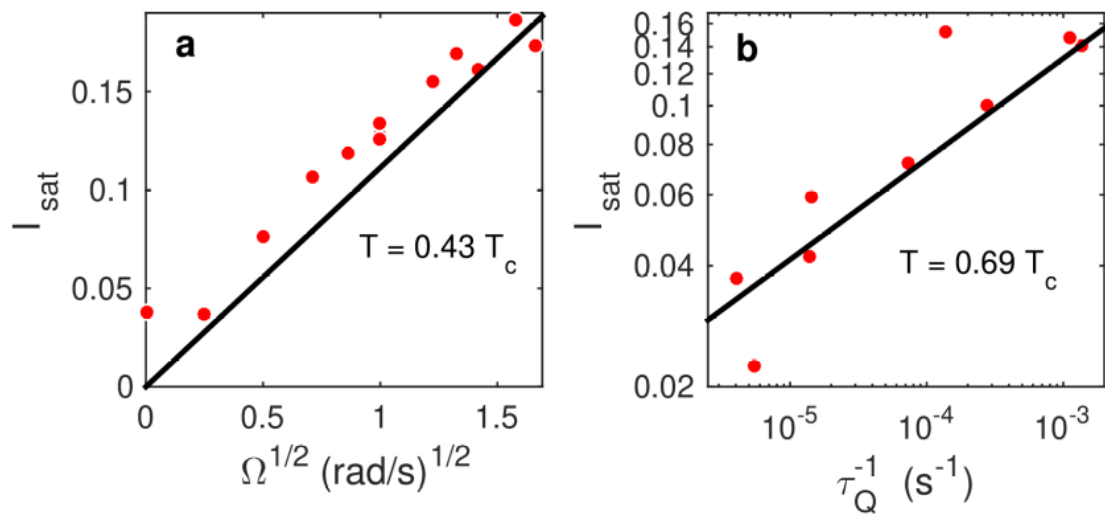


Half-quantum vortex

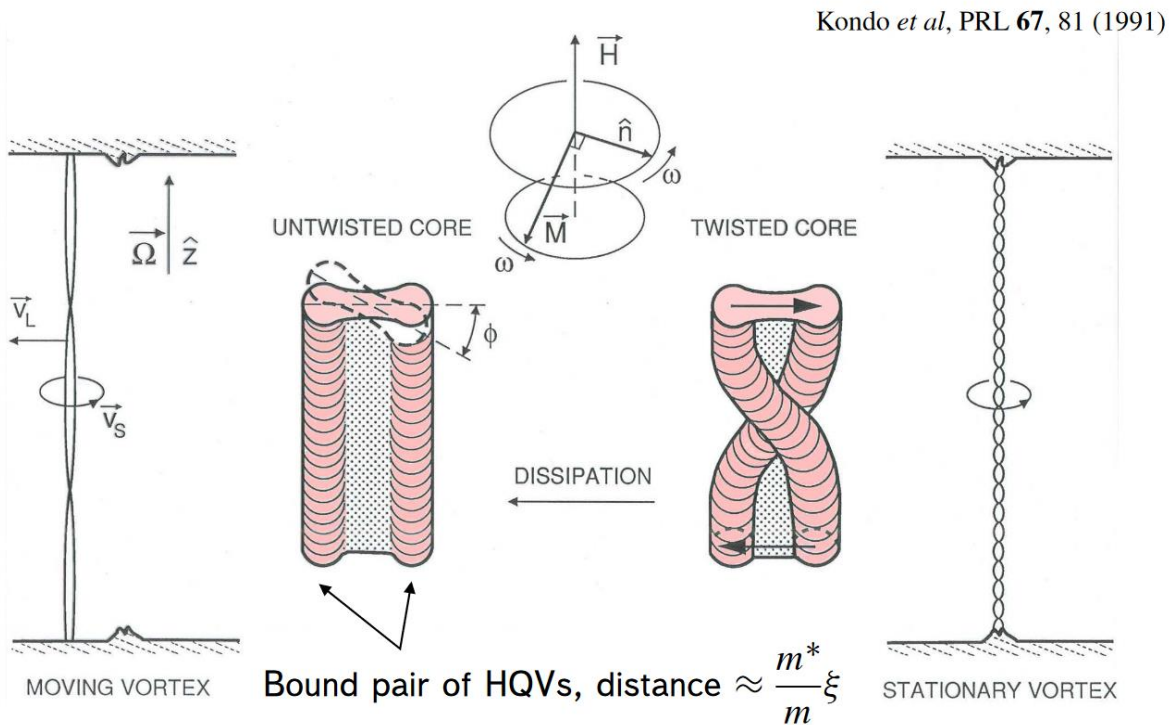
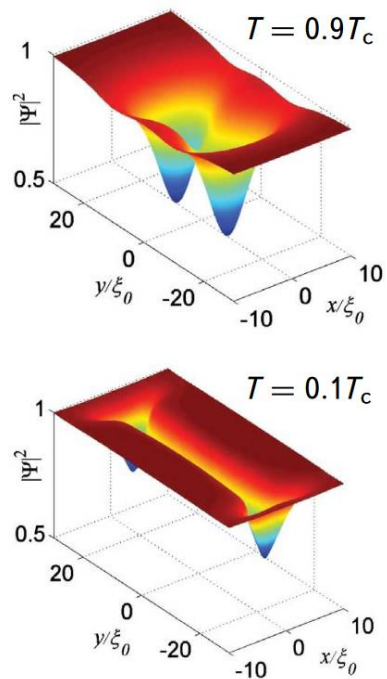
Single-quantum Half-quantum



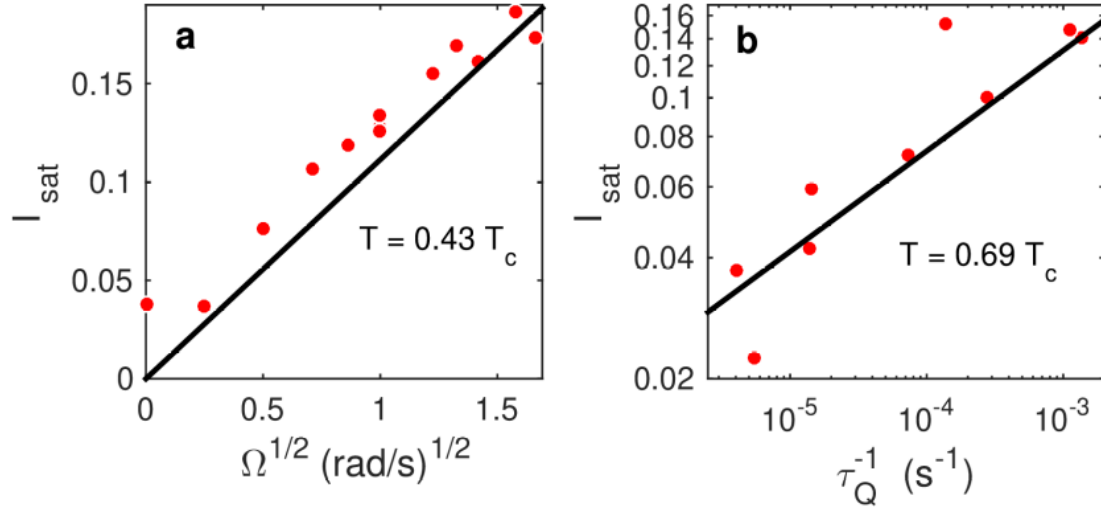
Half-quantum vortex



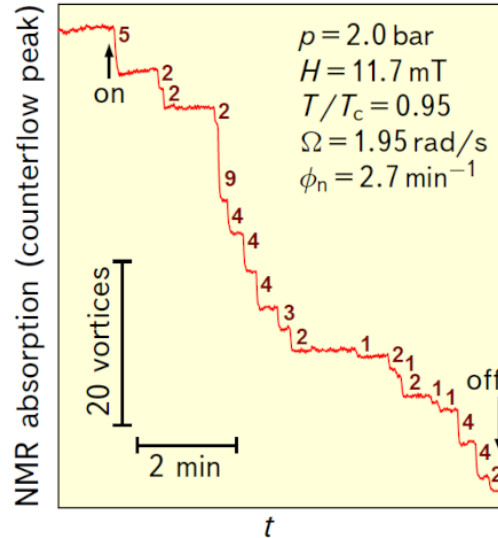
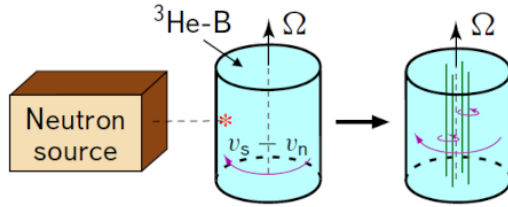
Double-core vortex in B phase



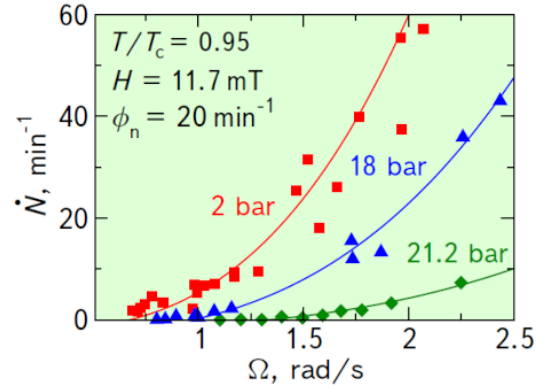
Half-quantum vortex



Kibble-Zurek mechanism



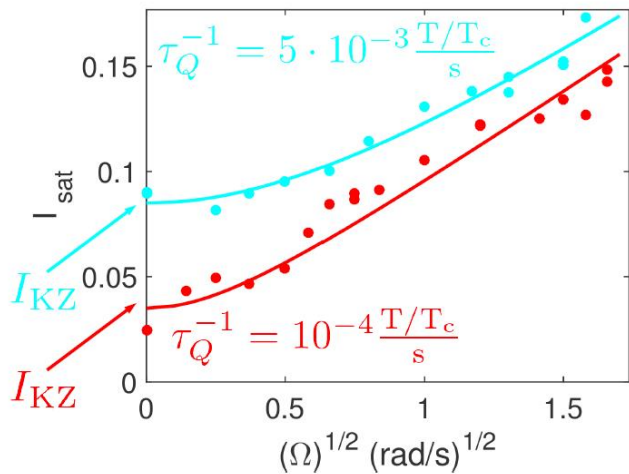
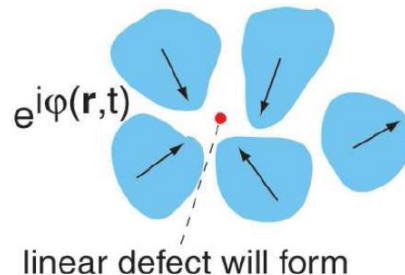
Vortex formation rate \dot{N} depends on p ,
 T , H , ϕ_n , $v_n = \Omega R$ and $v_s = \kappa N/2\pi R$



$$\frac{dN}{dt} = \phi_n \mathcal{A} \left[\left(\frac{v_n - v_s}{v_{\text{cn}}(p, T, H)} \right)^3 - 1 \right]$$

Kibble-Zurek combined with drive

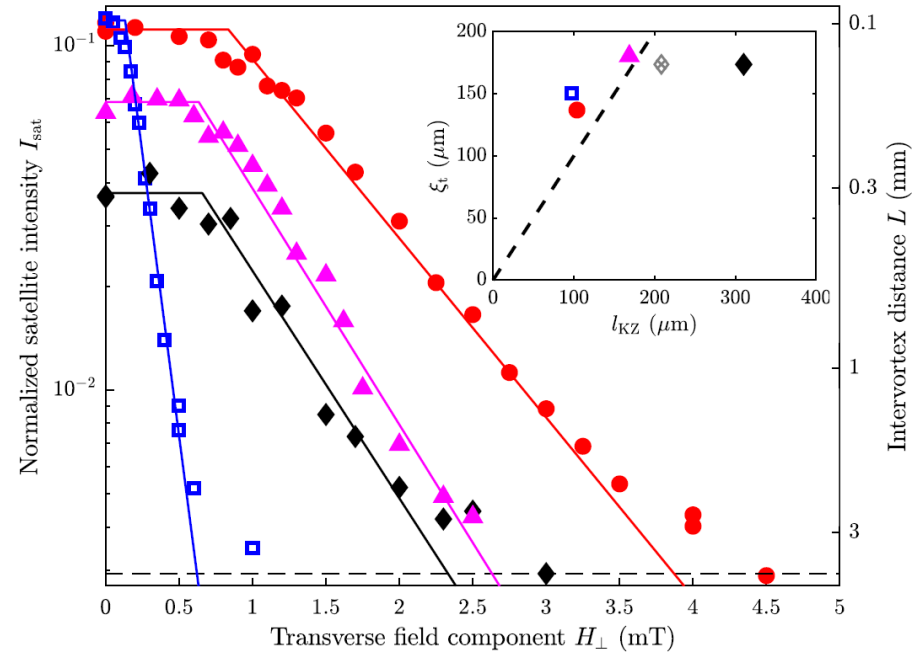
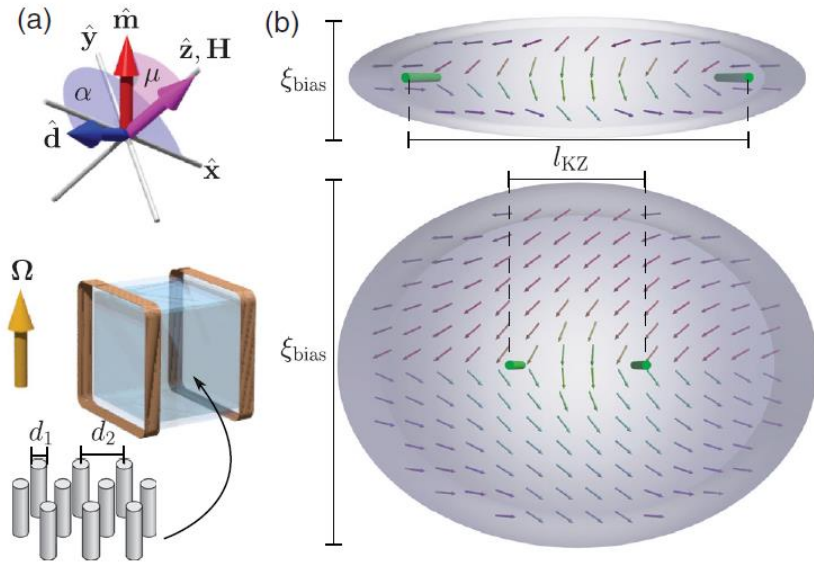
$$I_{\text{sat}} = \sqrt{I_{\text{KZ}}^2 + I_0^2 \Omega}$$



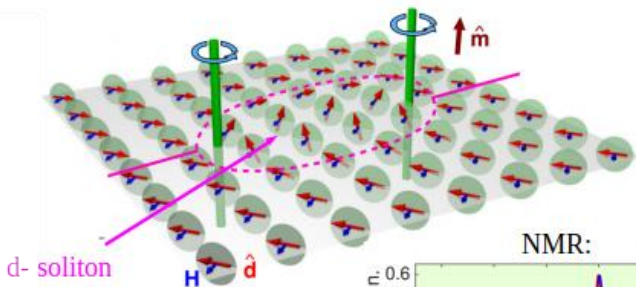
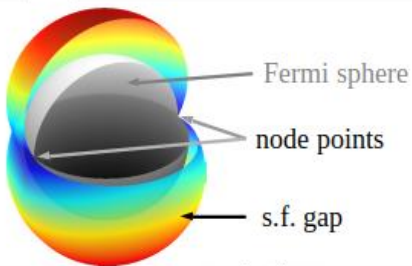
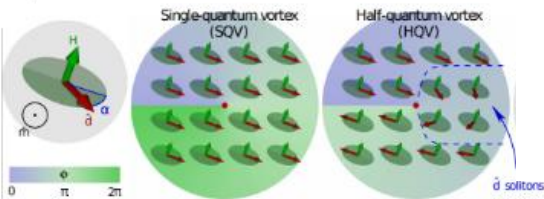
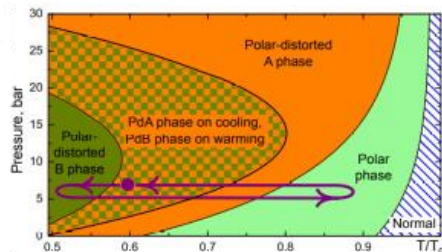
Apply:

- Rotation drive + weak KZ
- Rotation drive + large KZ

Kibble-Zurek suppressed with bias



Half-quantum vortex in the PdA phase

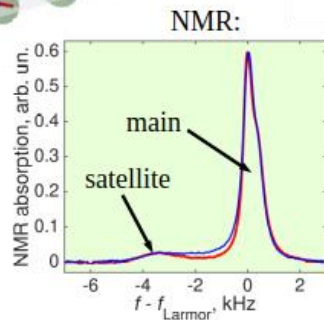


$$A_{\text{PdA}} = \Delta_{\text{PdA}} e^{i\varphi} \hat{\mathbf{d}}(\hat{\mathbf{m}} + i\hat{\mathbf{n}})$$

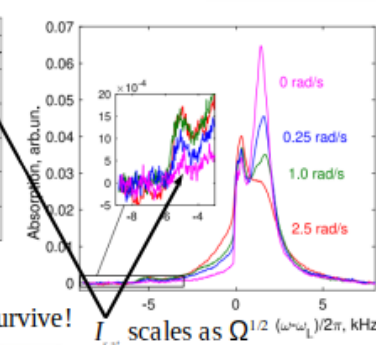
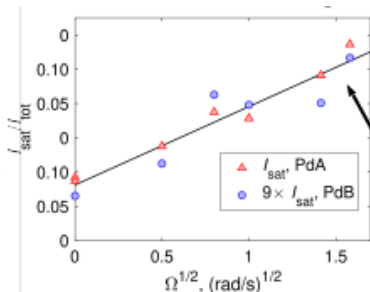
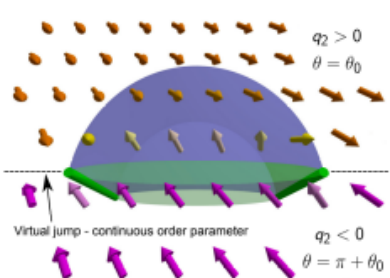
$\varphi \rightarrow \varphi + \pi$, $\hat{\mathbf{d}} \rightarrow -\hat{\mathbf{d}} \rightarrow$ OP remains singly valued \rightarrow HQVs

HQVs in $(p_x + ip_y)$ PdA phase:

[1] JTM, Dmitriev et al., Nat. Comm. **10**, 237 (2019)



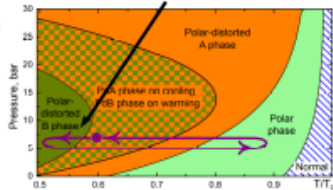
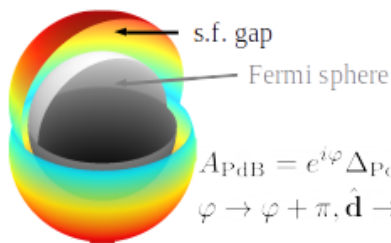
Half-quantum vortex in the PdB phase



Cosmology: Walls bounded by strings,
Kibble, Lazarides & Shafi, PRD **26** (1982)

HQVs prohibited, but survive!

I_{sat}^1 scales as $\Omega^{1/2}$ ($\omega = \omega_L$)/ 2π , kHz
→ from d -solitons!

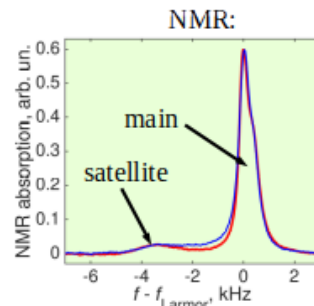


$$A_{\text{PdB}} = e^{i\varphi} \Delta_{\text{PdB}} (\hat{d}z + q_1 \hat{e}_1 x + q_2 \hat{e}_2 y)$$

$$\varphi \rightarrow \varphi + \pi, \hat{d} \rightarrow -\hat{d}, \hat{e}_1 \rightarrow -\hat{e}_1, \hat{e}_2 \text{ fixed: } q_2 \rightarrow -q_2$$

Walls bounded by strings in PdB phase:

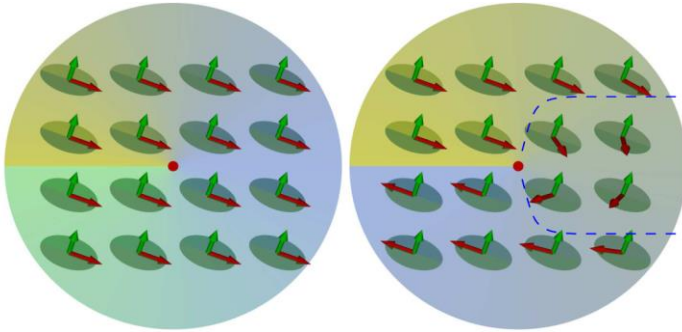
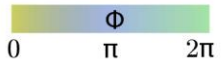
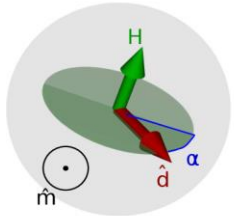
- [1] JTM, Dmitriev et al., Nat. Comm. **10**, 237 (2019)
- [2] Zhang, Phys. Rev. Research **2**, 043356 (2020)



Single-quantum vortex?

Single-quantum

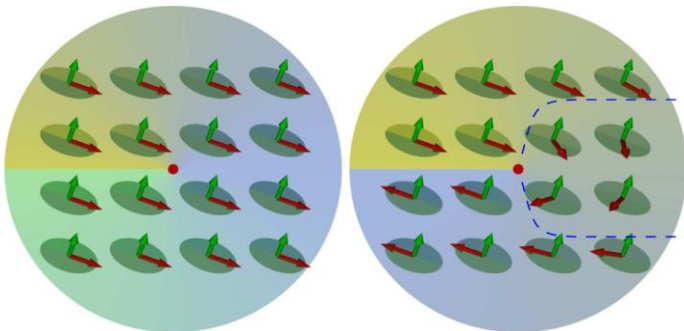
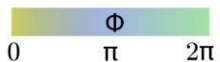
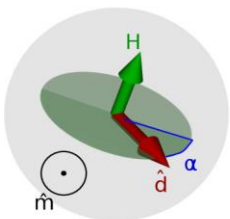
Half-quantum



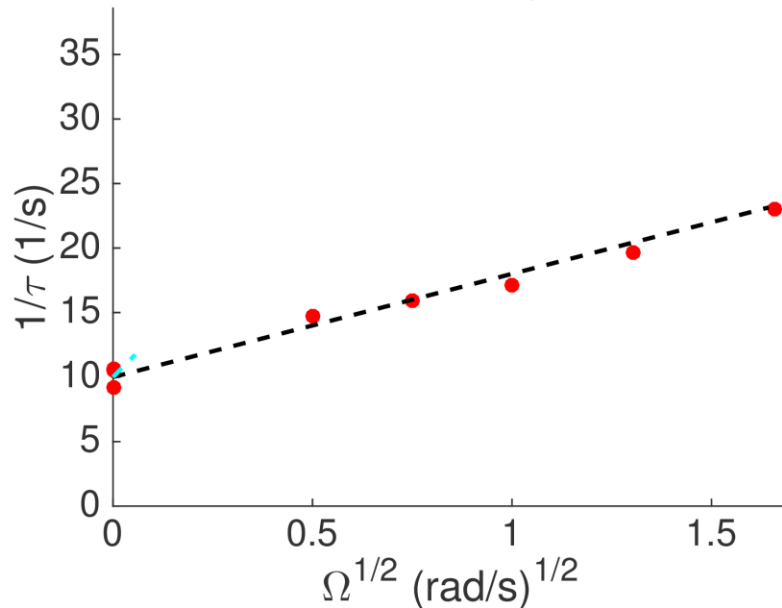
Single-quantum vortex?

Single-quantum

Half-quantum



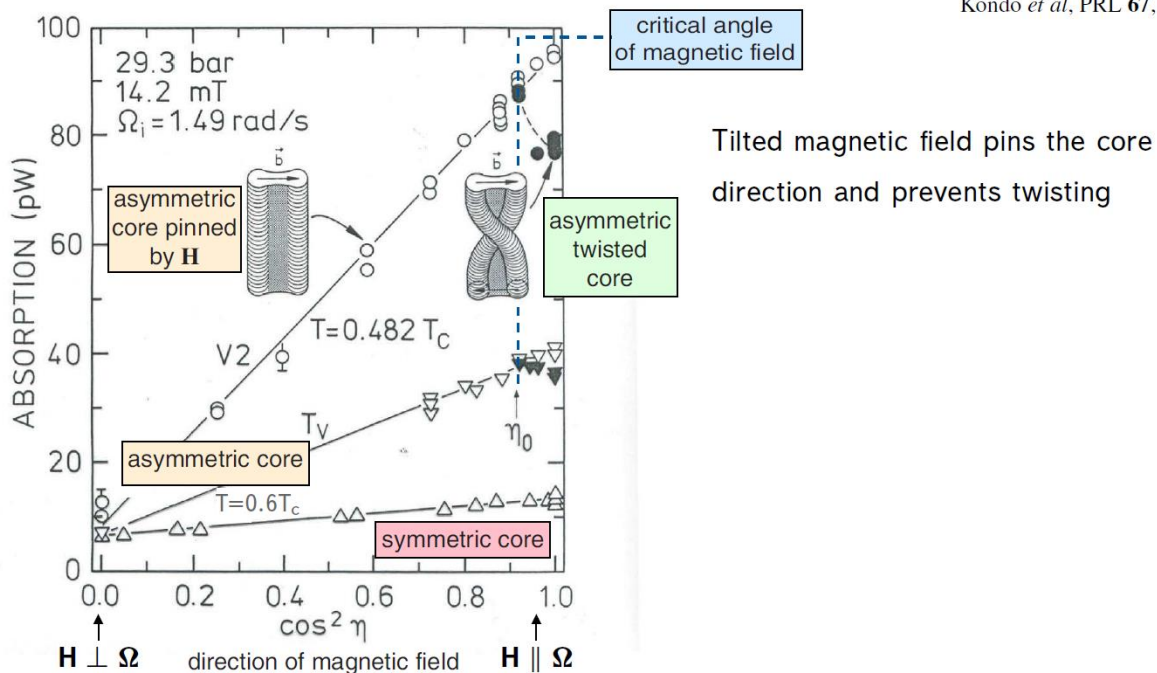
HPD relaxation, SQVs



Double-core vortex detected with HPD

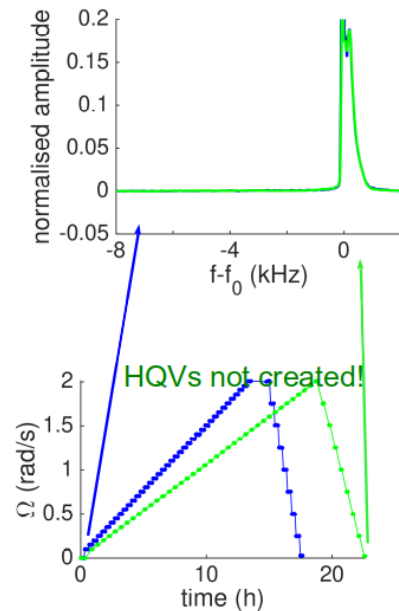
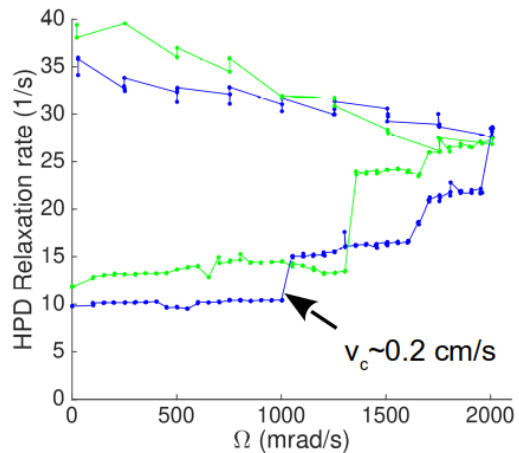
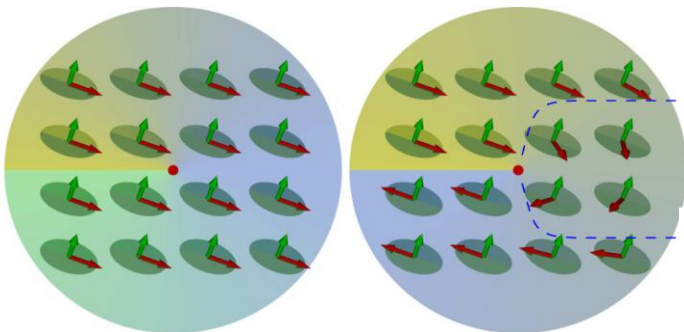
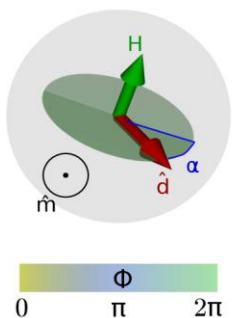
Twisting is observed as decrease of vortex contribution to the relaxation rate of magnon BEC.

Kondo *et al.*, PRL **67**, 81 (1991)

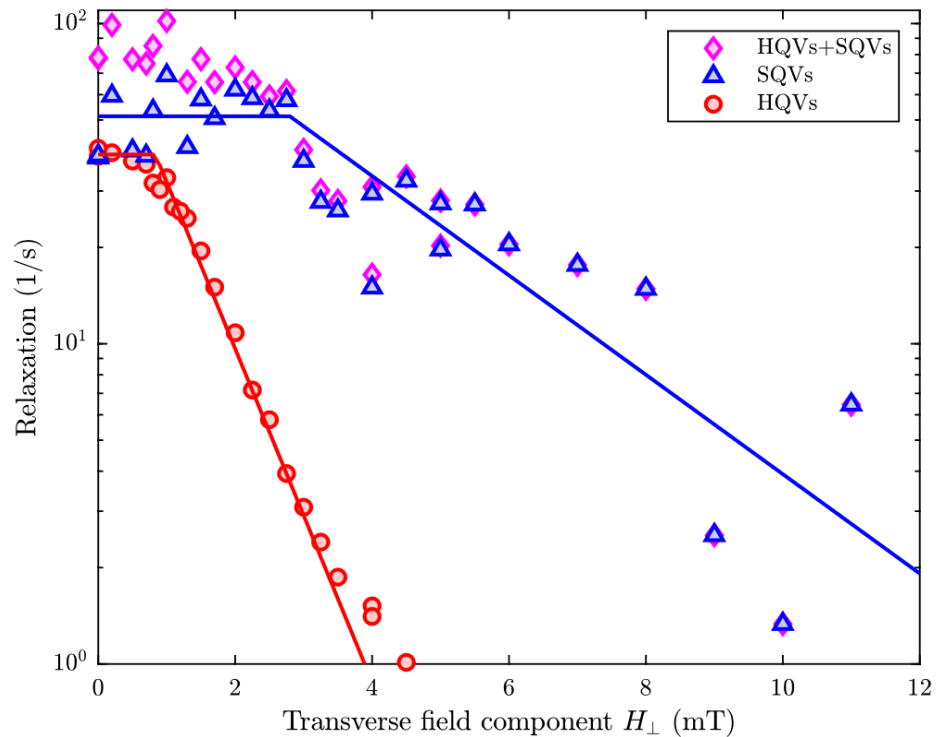
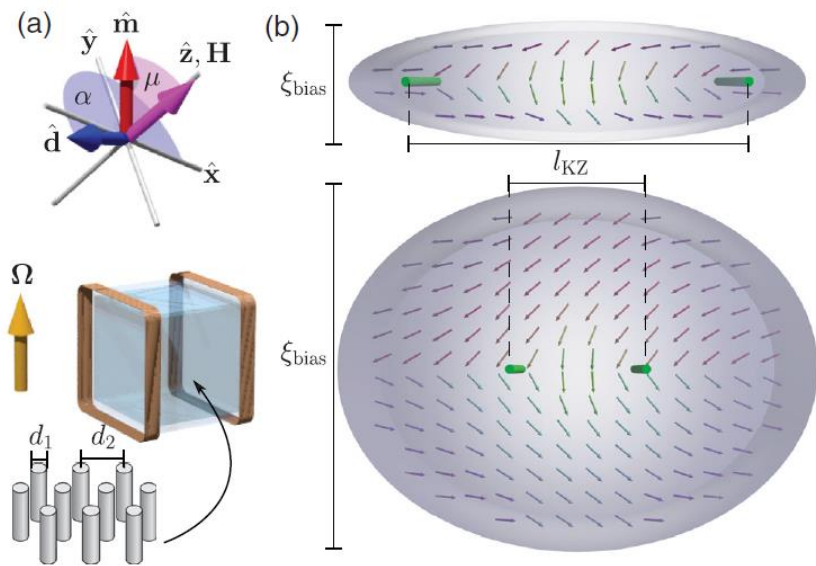


Single-quantum vortex?

Single-quantum **Half-quantum**

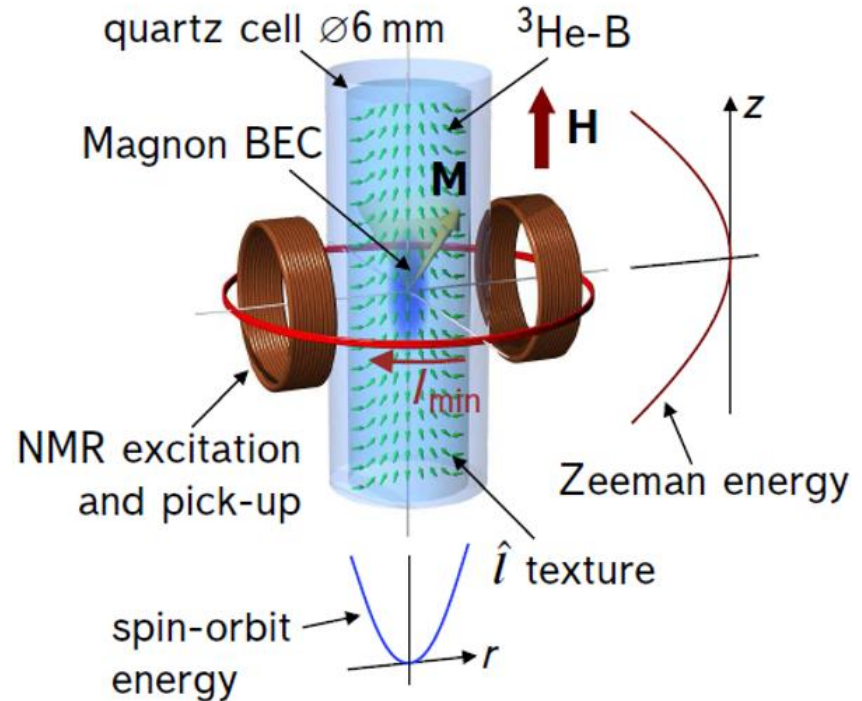


Kibble-Zurek suppressed with bias

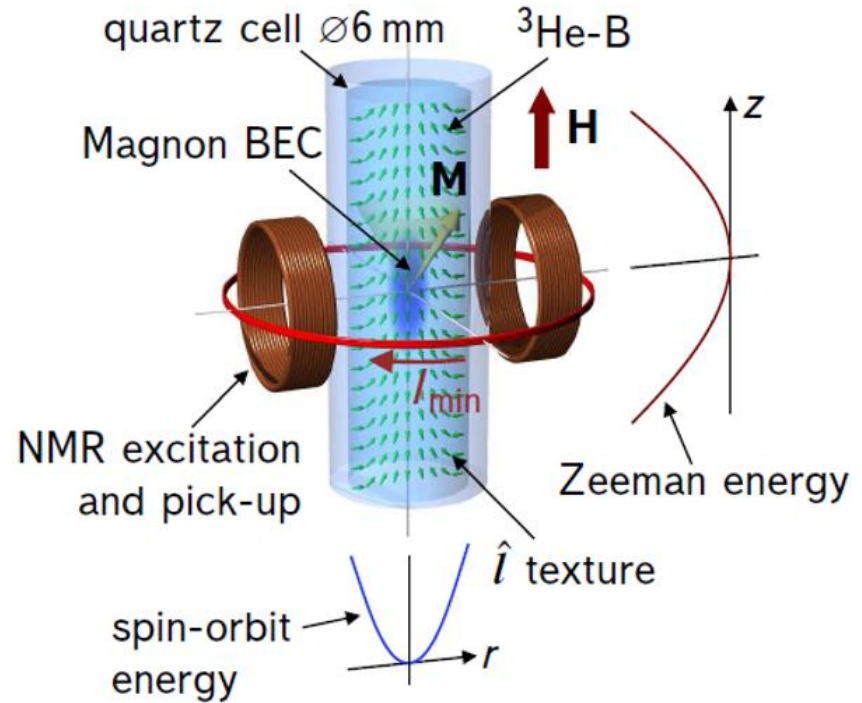
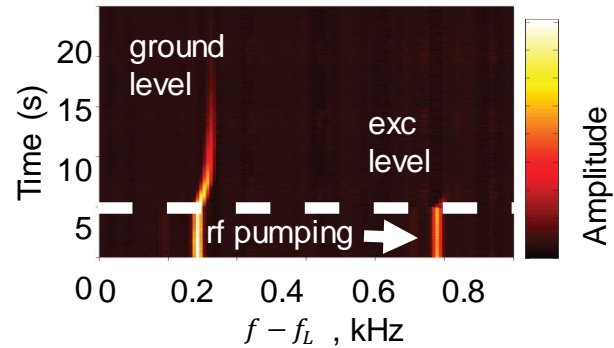


Trapped magnon BEC

PRL 108, 145303 (2012)
JETP letters 95, 544-548(2012)
JLTP 175 , 3-16 (2014)
JLTP 175 , 681-705 (2014)
JETP letters 101, 802-807 (2015)
Nature Communications 7, 1-6 (2016)
PRB 97, 014518 (2018)
PRL 120, 215301 (2018)
PRL 121, 025303 (2018)
Nature Materials 20, 171-174 (2021)
PRR 3, L032002 (2021)
Nature Communications 13, 1-9 (2022)



Trapped magnon BEC



Time Crystal?



Time crystals:
E.7 S.14 (1976)

Time Crystal?



Time crystals:
E.7 S.14 (1976)



F. Wilczek in PRL **109**,160401 (2012)

Time Crystal?



Time crystals:
E.7 S.14 (1976)



F. Wilczek in PRL **109**, 160401 (2012)



J. Davis

J. Pöllänen

Time Crystal?



Time crystals:
E.7 S.14 (1976)

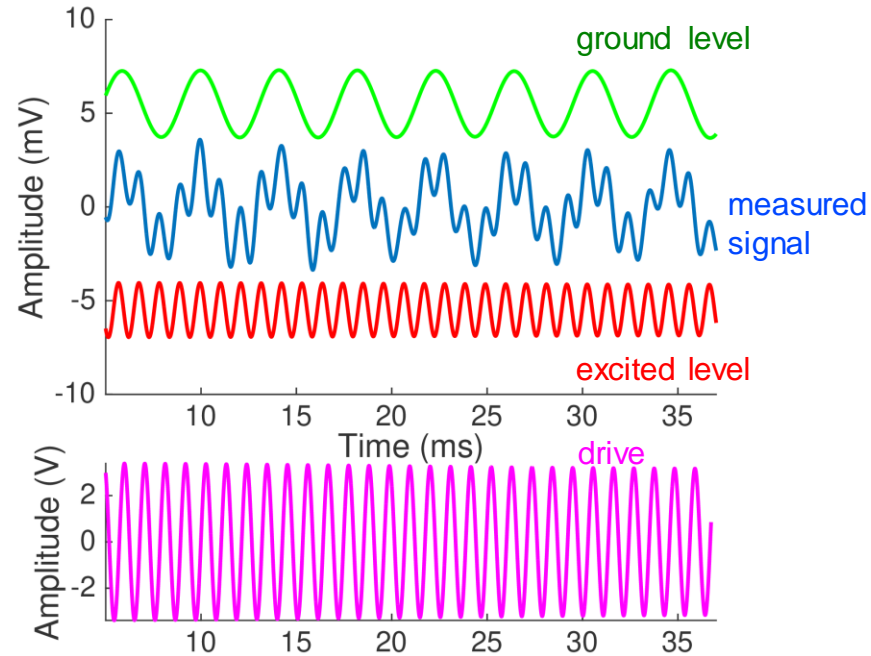
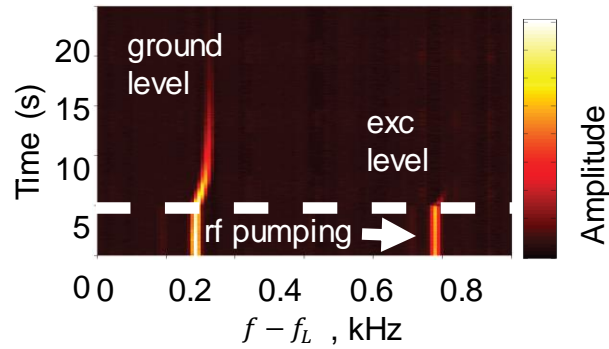


F. Wilczek in PRL **109**,160401 (2012)

- Phase of matter in repeating periodic motion
- Spontaneous period
- Cannot be observed in equilibrium (perpetual motion machine)

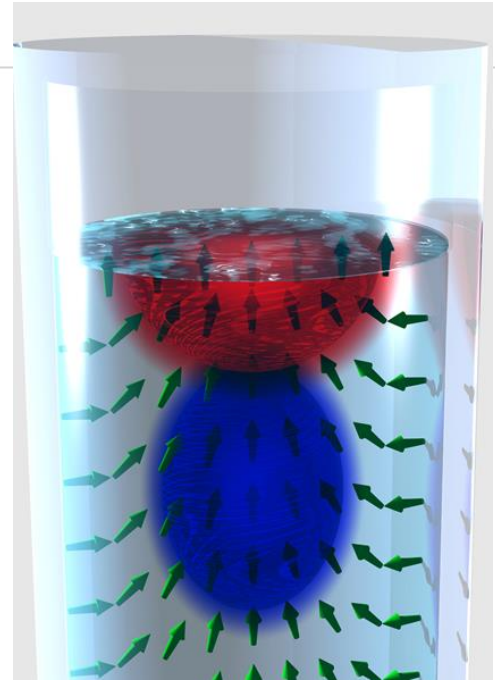
---> pumped / quasi-equilibrium many-body systems if observable

Time quasicrystal and continuous time crystal



Time crystal two-level system

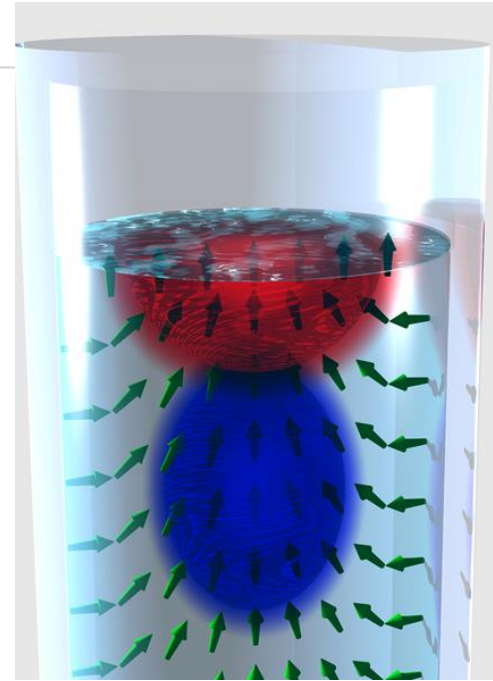
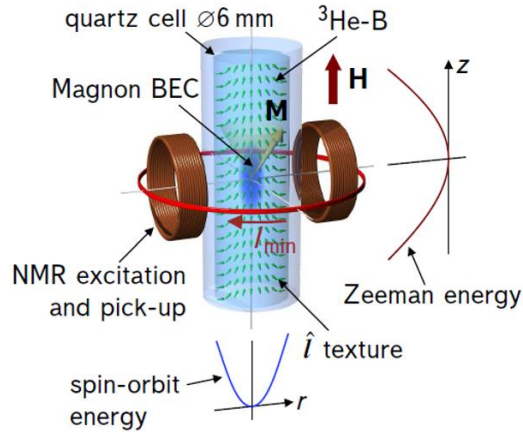
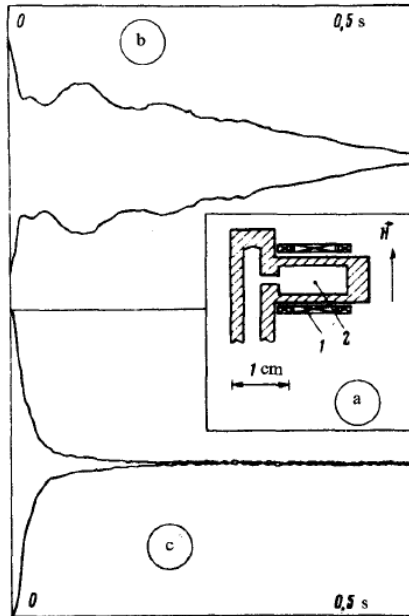
Nature M **20**, 171-174 (2021)
Nature Comms **13**, 3090 (2022)



$$\mathcal{H} = \hbar \begin{pmatrix} \omega_B[N_B(t)] & -\Omega \\ -\Omega & \omega_S \end{pmatrix}$$

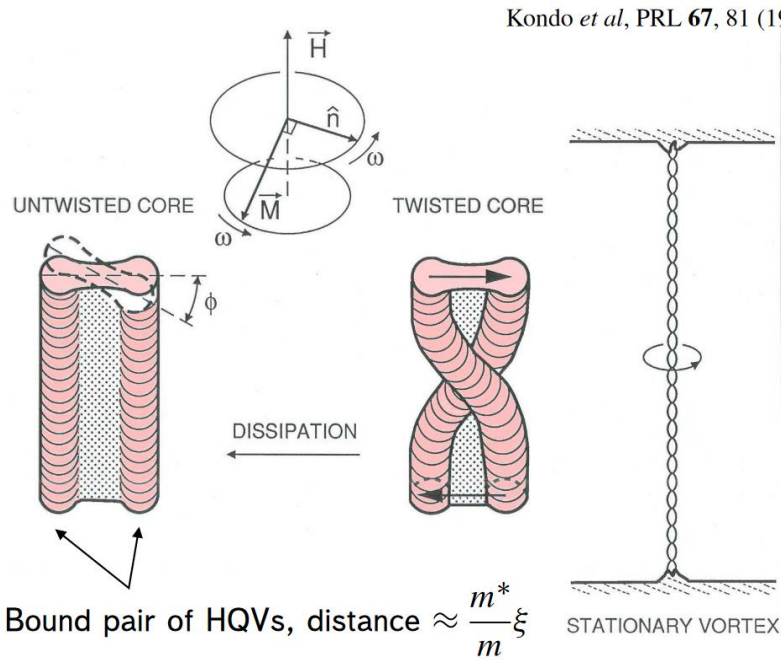
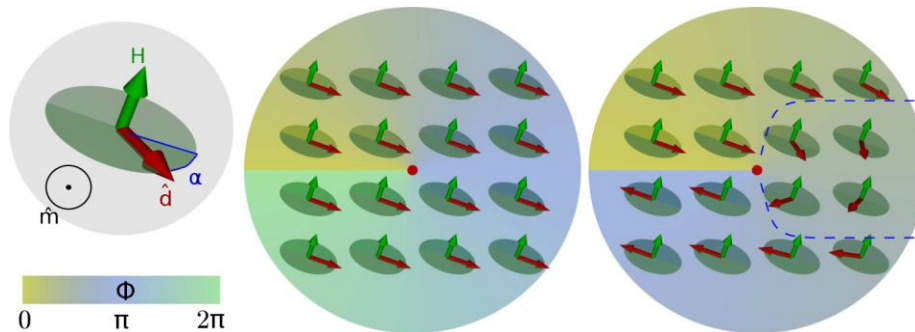
HPD, Magnon BEC or Time Crystal?

Nature M **20**, 171-174 (2021)
 Nature Comms **13**, 3090 (2022)



$$\mathcal{H} = \hbar \begin{pmatrix} \omega_B [N_B(t)] & -\Omega \\ -\Omega & \omega_S \end{pmatrix}$$

Thank you



Kondo *et al*, PRL **67**, 81 (1991)

